

## Solution Set of Inequalities

If two inequalities have the same solution set, they are said to be equivalent.

**Example:** Find the solution set of the following inequalities.

$$3x - 8 < x - 2$$

$$3x - 8 + 8 < x - 2 + 8$$

$$3x < x + 6$$

$$3x - x < x - x + 6$$

$$2x < 6$$

$$x < 6/2$$

$$x < 3$$

$$\delta = \{-\infty, 3\}$$

**Example:** Find the solution set of the following inequalities.

$$\left(\frac{2x-3}{x+2}\right) < \left(\frac{1}{3}\right) \quad x \neq -2$$

$$3(2x-3) < x+2$$

$$6x - 9 < x + 2$$

$$6x - 9 + 9 < x + 2 + 9$$

$$6x < x + 11$$

$$6x - x < x - x + 11$$

$$5x < 11$$

$$x < 11/5$$

$$\delta = (-2, 11/5)$$

Example: Find the solution set of the following inequalities.

$$x^2 - 3x + 2 < 0$$

$$(x-2)(x-1) < 0$$

$$x-2 < 0 \text{ or } x-1 < 0$$

$$\text{if } x-2 < 0 \rightarrow x-1 > 0$$

$$\text{if } x-2 > 0 \rightarrow x-1 < 0$$

$$\text{when } x-2 < 0 \rightarrow x < 2 \text{ and } x-1 > 0 \rightarrow x > 1 \rightarrow \delta = (1, 2)$$

$$\text{when } x-2 > 0 \rightarrow x > 2 \text{ and } x-1 < 0 \rightarrow x < 1 \rightarrow \delta = \emptyset$$

Example: Find the solution set of the following inequalities.

$$-x/3 < 2x + 1$$

$$-x < 6x + 3$$

$$-3 - x + x < 6x + x + 3 - 3$$

$$-3 < 7x$$

$$-3/7 < x$$

$$\delta = (-3/7, \infty)$$